

- Zero Order Moments Equations

$$\left\{ \begin{array}{l} \frac{\partial n_{cc}}{\partial t} = \frac{1}{q} \frac{\partial J_{cc}}{\partial x} + i \frac{\hbar P}{2m} \frac{\partial}{\partial x} (n_{cv} - n_{vc}) + \frac{P}{q} (J_{cv} + J_{vc}) \\ \frac{\partial n_{cv}}{\partial t} = \frac{1}{q} \frac{\partial J_{cv}}{\partial x} + \frac{i}{\hbar} [V_c(x, t) - V_v(x, t)] n_{cv} - i \frac{\hbar P}{2m} \frac{\partial}{\partial x} (n_{cc} + n_{vv}) + \frac{P}{q} (J_{cc} - J_{vv}) \\ \frac{\partial n_{vv}}{\partial t} = \frac{1}{q} \frac{\partial J_{vv}}{\partial x} + i \frac{\hbar P}{2m} \frac{\partial}{\partial x} (n_{cv} - n_{vc}) - \frac{P}{q} (J_{cv} + J_{vc}) \end{array} \right.$$

- First Order Moments Equations

$$\left\{ \begin{array}{l} \frac{\partial J_{cc}}{\partial t} = \frac{2q}{m} \frac{\partial \mathcal{E}_{cc}}{\partial x} + \frac{q}{m} V'_c(x, t) n_{cc} + i \frac{\hbar P}{2m} \frac{\partial}{\partial x} (J_{cv} - J_{vc} + \frac{2qP}{m} (\mathcal{E}_{cv} + \mathcal{E}_{vc})) \\ \frac{\partial J_{cv}}{\partial t} = \frac{2q}{m} \frac{\partial \mathcal{E}_{cv}}{\partial x} + \frac{q}{2m} [V'_c(x, t) + V'_v(x, t)] n_{cv} \\ \quad + i \frac{1}{\hbar} [V_c(x, t) - V_v(x, t)] J_{cv} - i \frac{\hbar P}{2m} \frac{\partial}{\partial x} (J_{cc} + J_{vv}) - i \frac{2qP}{m} (\mathcal{E}_{cc} - \mathcal{E}_{vv}) \\ \frac{\partial J_{vv}}{\partial t} = \frac{2q}{m} \frac{\partial \mathcal{E}_{vv}}{\partial x} + \frac{q}{m} V'_v(x, t) n_{vv} + i \frac{\hbar P}{2m} \frac{\partial}{\partial x} (J_{cv} - J_{vc}) - \frac{2qP}{m} (\mathcal{E}_{cv} + \mathcal{E}_{vc}) \end{array} \right.$$

- **Second Order Moments Equations**

$$\frac{\partial \mathcal{E}_{cc}}{\partial t} = -\frac{m}{2} \frac{\partial M_{cc}^{(3)}}{\partial x} + \frac{1}{q} V'_c(x, t) J_{cc} + i \frac{\hbar P}{2m} \frac{\partial}{\partial x} (\mathcal{E}_{cv} - \mathcal{E}_{vc}) - \frac{mP}{2} [M_{vc}^{(3)} + M_{cv}^{(3)}]$$

$$\begin{aligned} \frac{\partial \mathcal{E}_{cv}}{\partial t} = & -\frac{m}{2} \frac{\partial M_{cv}^{(3)}}{\partial x} + i \frac{\hbar}{8m} [V_v''(x, t) - V_c''(x, t)] n_{cv} + \frac{1}{2q} [V'_v(x, t) - V'_c(x, t)] \\ & - i \frac{1}{\hbar} [V_v(x, t) + V_c(x, t)] \mathcal{E}_{cv} - i \frac{\hbar P}{2m} \frac{\partial}{\partial x} (\mathcal{E}_{vv} + \mathcal{E}_{cc}) - i \frac{mP}{2} (M_{vv}^{(3)} - M_{cc}^{(3)}) \end{aligned}$$

$$\frac{\partial \mathcal{E}_{vv}}{\partial t} = \frac{m}{2} \frac{\partial M_{vv}^{(3)}}{\partial x} - \frac{1}{q} V'_v(x, t) J_{vv} - i \frac{\hbar P}{2m} \frac{\partial}{\partial x} (\mathcal{E}_{cv} - \mathcal{E}_{vc}) - \frac{mP}{2} [M_{cv}^{(3)} + M_{vc}^{(3)}]$$